

Arrays

1. Introduction to Arrays

- **Definition:**
An array is a collection of elements of the **same data type**, stored at **contiguous memory locations**, and accessed using an **index**.
- **Indexing:**
 - → Index starts from **0**.

Example:

```
int arr[5] = {10, 20, 30, 40, 50};  
// arr[0] = 10, arr[1] = 20, arr[2] = 30 ...
```

2. Features of Arrays

- Stores multiple values under one name.
- Fixed size (declared once).
- Fast access ($O(1)$) using index.
- Elements stored in contiguous memory.

3. Declaring and Initializing Arrays

Declaration

```
int arr[5];    // uninitialized array of size 5
```

Initialization (Static)

```
int arr[5] = {10, 20, 30, 40, 50};  
int arr[] = {1, 2, 3, 4};    // compiler decides size
```

Partial Initialization

```
int arr[5] = {10, 20};  
// arr[0]=10, arr[1]=20, arr[2]=0, arr[3]=0, arr[4]=0
```

4. Taking Input from User

```
#include <iostream>  
using namespace std;  
  
int main() {  
    int n;  
    cout << "Enter size of array: ";  
    cin >> n;  
  
    int arr[n];  
    cout << "Enter elements: ";  
    for(int i=0; i<n; i++) {  
        cin >> arr[i];  
    }  
  
    cout << "Array elements: ";  
    for(int i=0; i<n; i++) {
```

```
        cout << arr[i] << " ";  
    }  
    return 0;  
}
```

5. Traversal of Array

- Visiting each element once using loop.
- **Time Complexity:** $O(n)$.

```
for(int i=0; i<n; i++) {  
    cout << arr[i] << " ";  
}
```

6. Array Operations

(A) Insertion

At end:

```
arr[n] = value;
```

-
- At index: shift elements → costly operation $O(n)$.

(B) Deletion

- Remove element at index and shift left.

(C) Updation

```
arr[2] = 100; // updates 3rd element
```

(D) Searching

- **Linear Search** $\rightarrow O(n)$.
- **Binary Search** (only for sorted arrays) $\rightarrow O(\log n)$.

7. Memory Representation of Array

- Arrays are stored sequentially in memory.

Formula:

$\text{Address}(\text{arr}[i]) = \text{Base address} + (i * \text{size_of_each_element})$

- **Example:**
If base address = 1000, each int = 4 bytes $\rightarrow$
 - $\text{arr}[0] = 1000$
 - $\text{arr}[1] = 1004$
 - $\text{arr}[2] = 1008 \dots$

8. Types of Arrays

(A) One-Dimensional Array (1D Array)

Stores elements in a single row.

```
int arr[5] = {1, 2, 3, 4, 5};
```

(B) Two-Dimensional Array (2D Array or Matrix)

Stores elements in rows and columns.

```
int matrix[2][3] = {{1,2,3}, {4,5,6}};
```

(C) Multi-Dimensional Array

Arrays with more than two dimensions (rare).

```
int arr[3][3][3];
```

9. Advantages of Arrays

Random access ($O(1)$).
Easy to use and implement.
Best for storing fixed-size data.

10. Disadvantages of Arrays

Fixed size (cannot grow/shrink).
Insertion/Deletion is costly ($O(n)$).
Wastage of memory if array is not full.

11. Complexity Analysis

Operation	Time Complexity
Traversal	$O(n)$
Insertion (at end)	$O(1)$
Insertion (at position)	$O(n)$
Deletion	$O(n)$
Searching (Linear)	$O(n)$
Searching (Binary, Sorted)	$O(\log n)$